

6.2 Products and Factors

1)

$$\begin{array}{c}
 \begin{array}{|c|c|}
 \hline
 x & + & 5 \\
 \hline
 3 & & 3*(x+5) \\
 \hline
 \end{array}
 = 3 \begin{array}{|c|}
 \hline
 x \\
 \hline
 3x \\
 \hline
 \end{array}
 + 3 \begin{array}{|c|}
 \hline
 5 \\
 \hline
 15 \\
 \hline
 \end{array}
 \end{array}$$

$3(x+5) = 3x + 15$

3)

$$\begin{aligned}
 & 8z * (5z - 3) \\
 & = (8z * 5z) - (8z * 3) \\
 & = 40z^2 - 24z
 \end{aligned}$$

5)

$$\begin{aligned}
 & -(-x^2 + 9x - 5) \\
 & = (-1) * (-x^2 + 9x - 5) \\
 & = x^2 - 9x + 5
 \end{aligned}$$

7)

a)

$$\begin{array}{c}
 \begin{array}{|c|c|}
 \hline
 ? & ? \\
 \hline
 ? & 10x & -6 \\
 \hline
 \end{array}
 = 2 \begin{array}{|c|}
 \hline
 5x & + & -3 \\
 \hline
 10x & - & 6 \\
 \hline
 \end{array}
 \end{array}$$

$$10x - 6 = 2 * (5x + -3) = 2(5x - 3)$$

b) $2*(5x - 3) = (2*5x) - (2*3) = 10x - 6$

9)

a) $GCF(9x^3, 18x^5) = 9x^3$

b) $GCF(21x^2y, 15xy^3) = 3xy$

11) Surface Area = $2\pi r h + 2\pi r^2 = 2\pi r(h + r)$

13)

a) The expression has two terms because an addition sign separates them.

b) $(x + 3)$

c) $(x + 3) * 4y + (x + 3) * 9 = (x + 3) * (4y + 9) = (x + 3)(4y + 9)$

15)

a) $x^2 + 4x = 0$

$$x(x + 4) = 0$$

$$x = 0 \text{ or } x + 4 = 0$$

$$x = 0 \text{ or } x = -4$$

b)

$$x^2 - 11x = 0$$

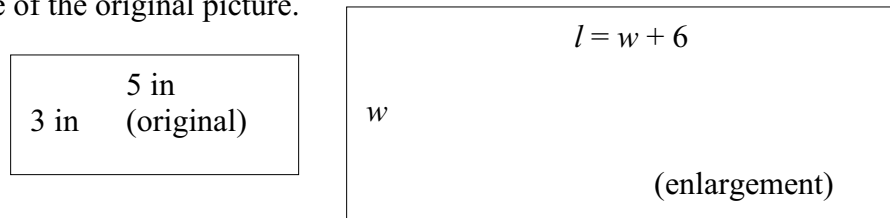
$$x(x - 11) = 0$$

$$x = 0 \text{ or } x - 11 = 0$$

$$x = 0 \text{ or } x = 11$$

Skill and Review

- 17) Let l be the length of the enlargement and let w denote its width.
We know $l = w + 6$. The dimensions of the enlarged picture are proportional to those of the original picture.



From this, we have $\frac{3}{5} = \frac{w}{w + 6}$. From this ratio and the cross multiplication property of proportions [FACT 5.1], we have $3(w + 6) = 5w$

$$3w + 18 = 5w$$

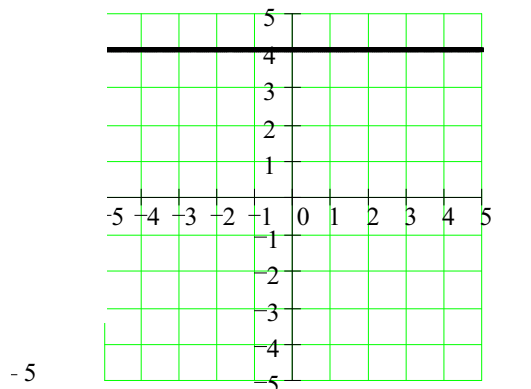
$$2w = 18$$

$$w = 9 \text{ in} \rightarrow l = (9 \text{ in}) + 6 \text{ in} = 15 \text{ in.}$$

The width of the enlargement is 9 in and the length is 15 in.

Note: There are several other proportions that can be constructed that would also yield the same answer.

- 19) a) Any ordered pair of the form $(x, 4)$ is acceptable, where x is any real number.



- b) Any ordered pair of the form $(-2, y)$ is acceptable, where y is any real number.

